

Modern Psychometric Approaches for Diagnostic Assessment

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Agenda

- What is Diagnostic Assessment?
- Where and how is it used?
- What kinds of information do we get from diagnostic assessments?
- What kinds of models are used to estimate attribute profiles?
- What are the basic specifications and characteristics of these models?
- What do these models look like in practice?
- How can these models be extended?
- What software do I need in order to use these models in my own research?
- Where can I find more information?

What is Diagnostic Assessment?

Diagnostic Assessment

- Assessment: A systematic procedure for collecting information that can be used to make inferences about the characteristics of people or objects (*Standards*, 2014).
- Diagnostic Assessment: An assessment procedure whose goal is to make classification-based (i.e., categorical) decisions (diagnoses) about individuals.
- Represents an evolution in psychometrics from test scores (CTT) → individual item responses (IRT) → individual components of items/tasks (de la Torre et al., 2017)

Diagnostic Assessment

- Diagnostic assessments yield (Carragher et al., 2019):
 - Information on multiple skills
 - Grouping of respondents with similar profiles
 - The ability to adapt assessment based on skill profiles
- Whereas traditional assessments (CTT, IRT) are typically focused on scores and rankings, diagnostic assessments are concerned with classifying (e.g., master/non-master, proficient/not proficient, presence/absence, etc.)
- Typically applied to low-stakes assessment scenarios
 - Lack of literature on psychometric properties of models

How are diagnostic assessments used?

Diagnostic Assessment – Applications

- Educational assessment
 - Modeling mastery of fine-grained competencies
 - Using patterns of misconceptions to choose targeted interventions
 - Implementing adaptive testing at a higher resolution than is typical with IRT-based CAT
 - Trade-off: Inferences will be for a much narrower domain
- Clinical assessment
 - Modeling potential diagnoses (profiles) as a function of individual symptoms
 - Choosing interventions based on behavior profiles

Diagnostic Assessment – Applications

- I/O psychology
 - Modeling workplace competencies and then using the resulting profiles to match applicants to positions
 - Identifying employees with particular patterns of deficiencies in order to provide customized professional development

What kinds of information do we get from diagnostic assessments?

Attribute Profiles

- Diagnostic assessment provides estimates of skill status as well as pattern classifications known as attribute profiles.
- Attribute profiles are patterns of classification on the latent variables representing the skills being assessed.
 - For example, you might see [0, 0, 1, 0] used to represent an attribute profile corresponding to non-mastery on skills 1, 2, and 4 but mastery of skill 3.
- These profiles might offer additional information beyond the individual latent skill classifications (i.e., interactions).
- Attribute profiles can represent complex hypotheses about the relationships between the latent skills (e.g., attribute hierarchies).



DiagnOsis scoring report

Student Name: Margo

LanguEdge Reading Comprehension Test 1

Review Your Answers

Question	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37
Your Answer	✓	✓	✓	2	✓	1	4	✓	✓	✓	3	2	2	✓	✓	✓	✓	2	✓	✓	✓	3	2	3	5	1	✓	1	4	4	✓	✓	✓	o	✓	3	1,4,6 2,3
Correct Answer	2	3	2	3	3	3	1	1	1	4	4	3	2,4,6	2	3	2	1	3	2	3	4	2	4	1	1,5,6	4	2	2	3	3	1	2	2	2	4	1	1,5,6 3,7
Difficulty	e	m	e	h	m	m	h	h	m	m	h	m	m	e	m	m	m	e	e	e	e	h	m	m	m	m	e	h	m	e	e	e	e	m	h	m	h

Scoring

Correct answer to questions with 4 choices = Plus 1 point
Wrong or omitted answer = No point
Q13 & 25: 3 correct = 2 points, 2 correct=1 point
Q37: 5 correct=3 points, 4 correct=2 points, 3 correct = 1 point

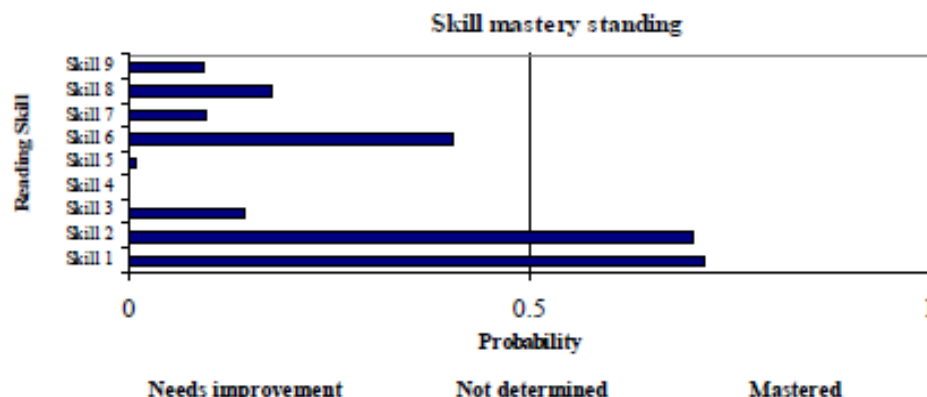
Key

✓ Correct
o Omitted
+ Plus partial points
e = Easy, m = Medium, h = Hard
(Difficulty is based on 1372 students' performance on this test)

Score

You earned **20** out of maximum **41** points.
10 points from **12** easy questions
7 points from **17** medium questions
3 points from **8** hard questions
You omitted 1 question.

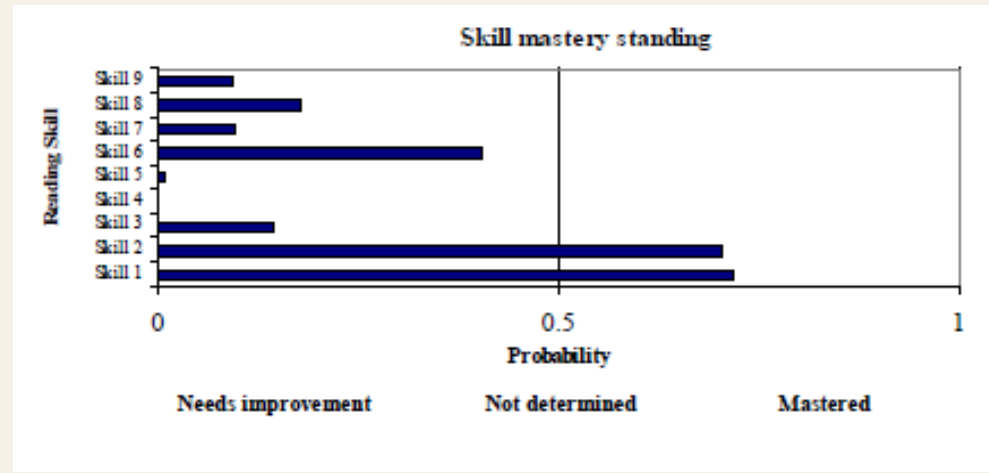
Improve Your Skills



How to Interpret Skill Mastery

- Nine primary reading skills are assessed in this reading comprehension test. Please review skill descriptions and example questions attached to this scoring report.
- The graph on the left side shows your probable mastery standing of each skill.
- The grey region indicates that your probable mastery standing cannot be determined.
- There may be some measurement error associated with the classification.
- This diagnostic information can be more useful when used in combination with your teacher's and your own evaluation of your reading skills.

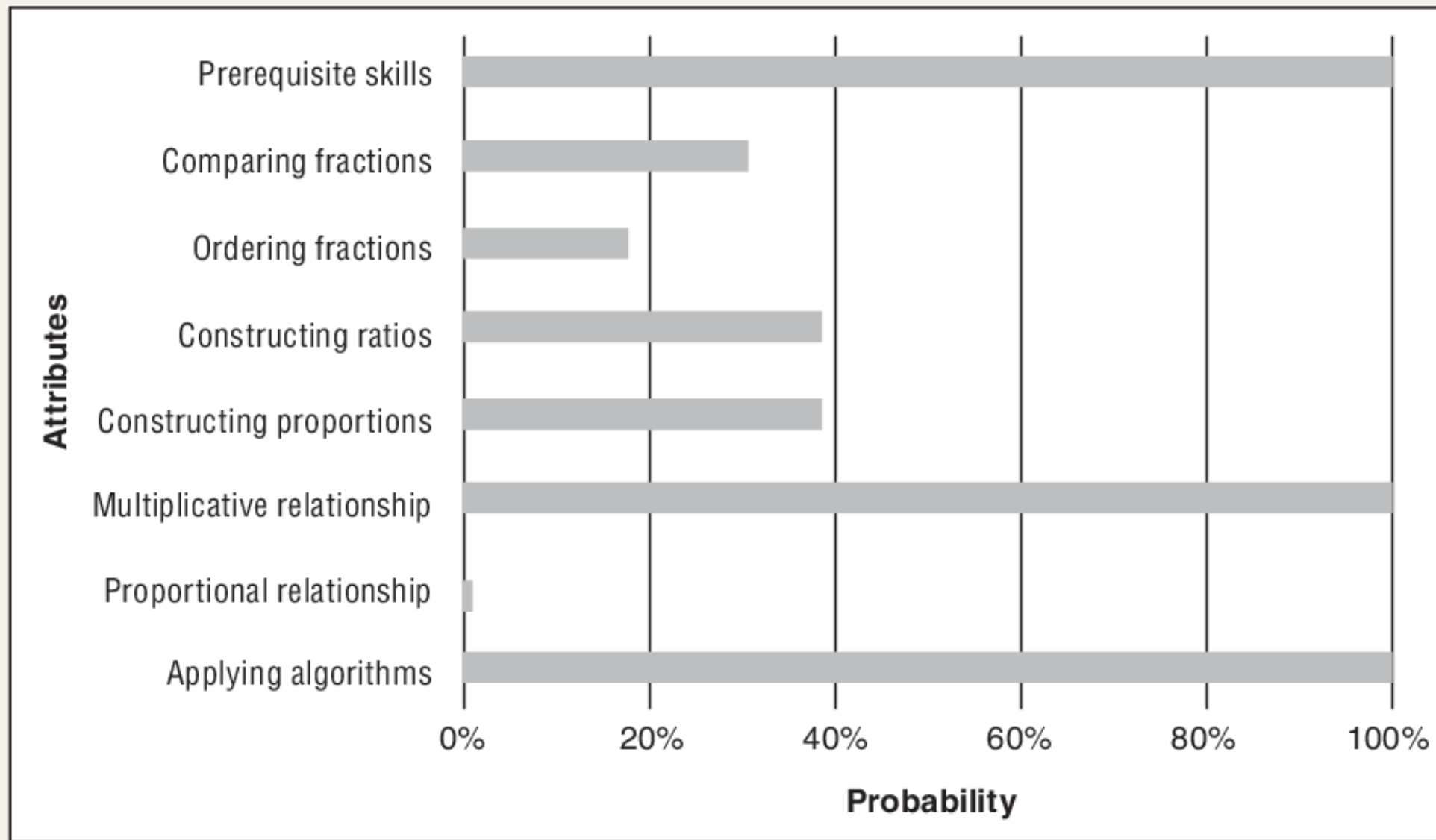
Source: Jang (2005)



We can apply a cut-off rule where Mastery is $\geq 60\%$, Non-mastery is $\leq 40\%$, values $>40\%$ but $<60\%$ are *indifferent*...

Skill 1	Skill 2	Skill 3	Skill 4	Skill 5	Skill 6	Skill 7	Skill 8	Skill 9
😊	😊	😞	😞	😞	😐	😞	😞	😞

Source: Jang (2005)



Source: de la Torre et al. (2017)

How do we model attribute profiles?

Modeling Attribute Profiles

- There are two dominant frameworks used for modeling attribute profiles:
 - Diagnostic classification models (DCM)
 - Bayesian networks (BN)
- Really there's just one “dominant” framework but I like Bayes nets, so...
- These models have a lot in common:
 - DCM can, in most cases be considered as a special case of a BN
 - Both tend to be entirely categorical (commonly, binary OVs and categorical LVs)
 - There are exceptions such as the HDCM models (de la Torre & Douglas, 2004; Templin & Bradshaw, 2014).
 - Not that dissimilar from LCA / LTA models in the most basic sense
 - Cross-sectional DCMs are often formulated as something akin to a confirmatory LCA with 2^A latent classes.

Diagnostic Classification Models

- DCM are a family of models that classify respondents into classes
 - Classes are mutually exclusive
- Also referred to as: cognitive diagnosis/diagnostic models, latent response models, structured IRT models, cognitive psychometric models, ...
- DCMs can be thought of as constrained, or confirmatory latent class models
 - 2^A possible classes (for binary LVs) where A is the number of skills contributing to the profile
 - EX: a model with four skills will have $2^4=16$ possible profiles that examinees can be classified into.
- DCMs model responses to categorical (typically dichotomous) items as a function of discrete latent skill variables
- The measurement model is defined by a Q-matrix...

Diagnostic Classification Models

	Skill1	Skill2	Skill3	Skill4
Item1	1	0	0	0
Item2	1	0	0	0
Item3	1	0	0	0
Item4	1	1	0	0
Item5	1	0	1	0
Item6	0	1	0	0
Item7	0	1	0	0
Item8	0	1	0	0
Item9	0	1	1	0
Item10	0	1	0	1
Item11	0	0	1	0
Item12	0	0	1	0
Item13	0	0	1	0
Item14	0	0	1	1
Item15	1	0	1	0
Item16	0	0	0	1
Item17	0	0	0	1
Item18	0	0	0	1
Item19	1	0	0	1
Item20	0	1	0	1

Diagnostic Classification Models

- The probability of a correct response depends on the estimated proficiency for the skills represented by that item (LCDM formulation)

$$P(\text{correct}) = \text{intercept} + \text{main skill effect}(s) + \text{interactions}$$

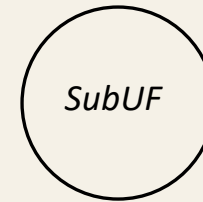
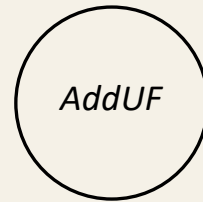
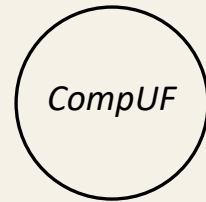
- There are several (and I mean SEVERAL) models in the DCM family which are separated by the assumptions they make about how skills interact to influence task performance
- DINA, DINO, NIDA, NIDO, C-RUM, R-RUM, LCDM, G-DINA, GDM, etc.

Diagnostic Classification Models

- Constructing a DCM typically requires four steps (Rupp, Templin, & Henson, 2010):
 - Identifying the target constructs (latent attributes)
 - Specifying the observed variables (items, tasks)
 - Linking the observed variables to the latent attributes (measurement model)
 - Specifying the relationship among the latent attributes (structural model; e.g., conjunctive [AND], disjunctive [OR], saturated, etc.)

DCM – Basic Example

- Assume we have three skills: comparing, adding, and subtracting unit fractions



DCM – Basic Example

- $J = 9$

- Q-matrix:

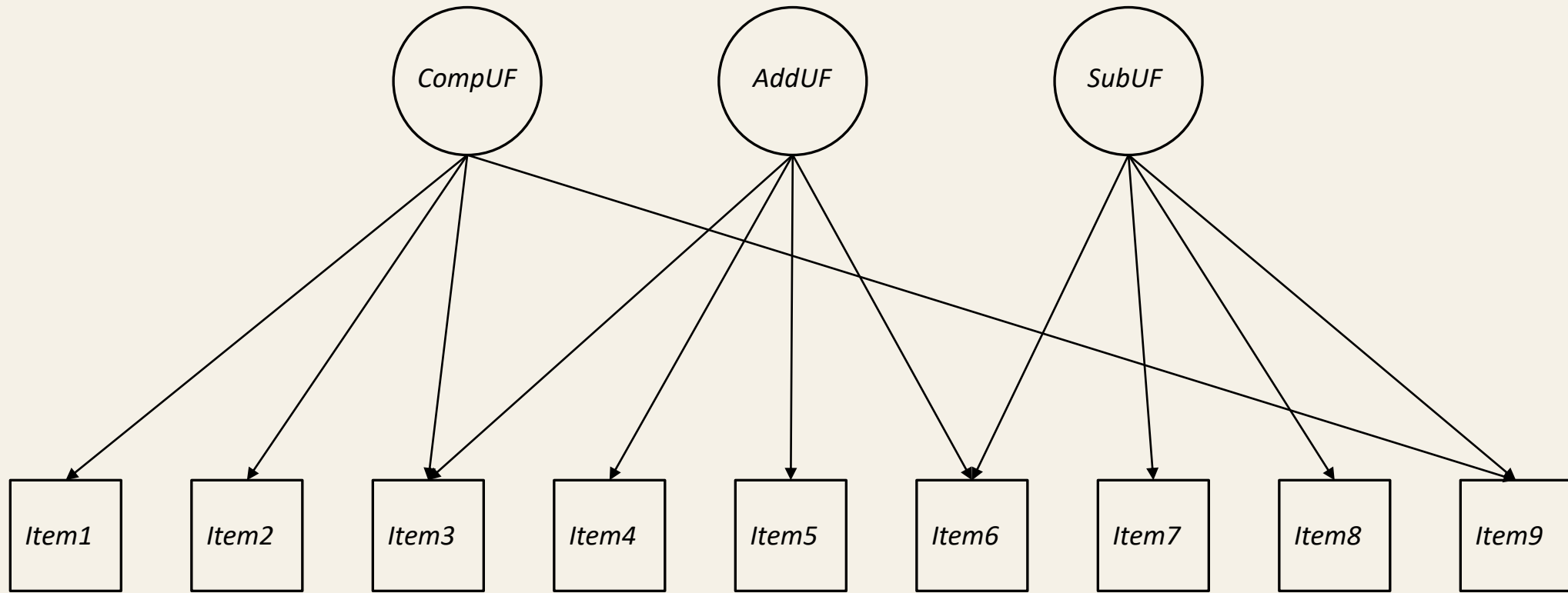
	Comparing UF	Adding UF	Subtracting UF
Item1	1	0	0
Item2	1	0	0
Item3	1	1	0
Item4	0	1	0
Item5	0	1	0
Item6	0	1	1
Item7	0	0	1
Item8	0	0	1
Item9	1	0	1

DCM – Basic Example

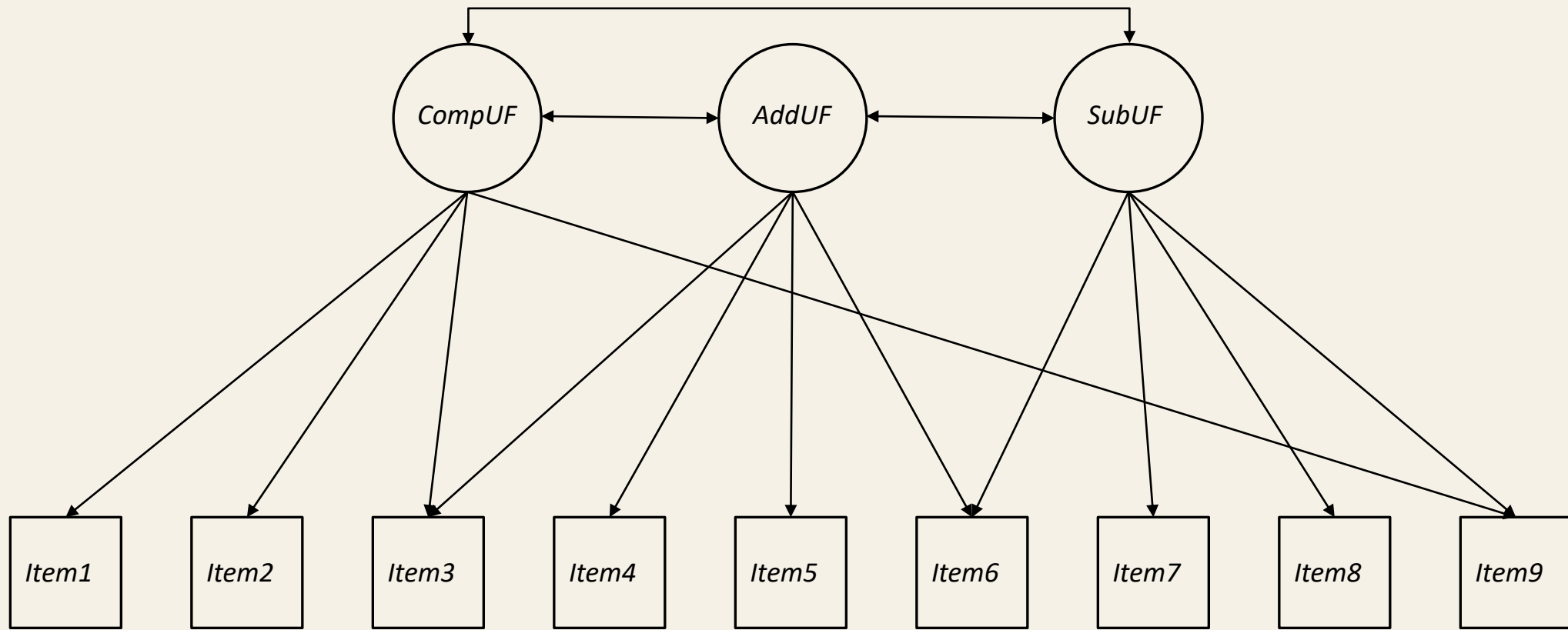
- $2^A = 2^3 = 8$ skill profiles

[0,0,0]	[1,0,0]
[0,0,1]	[1,1,0]
[0,1,0]	[1,0,1]
[0,1,1]	[1,1,1]

DCM – Basic Example



DCM – Basic Example



DCM – Basic Example

- Items 3, 6, and 9 assess two skills
- Loglinear model (LCDM):
 - Success on these items is modeled as a function of the main effect of each skill and the interaction between the two skills
- Disjunctive model (e.g., DINO):
 - Guessing parameter: those who haven't mastered either skill
 - Slipping parameter: those who have mastered at least one skill
- Conjunctive model (e.g., DINA):
 - Guessing parameter: those who have mastered <2 skills
 - Slipping parameter: those who have mastered both skills

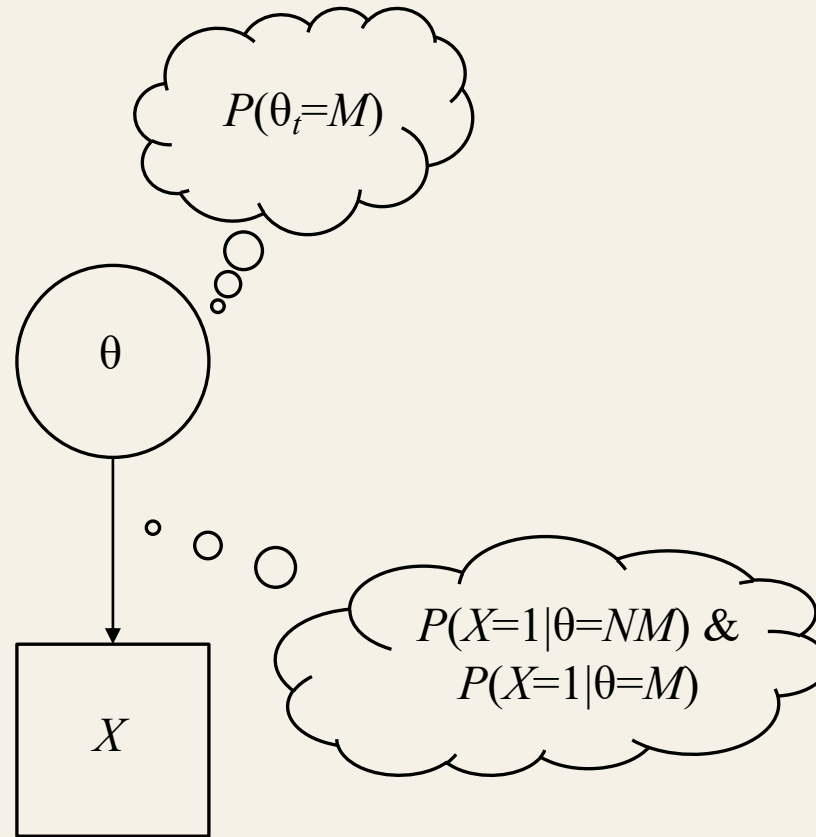
Bayesian Networks

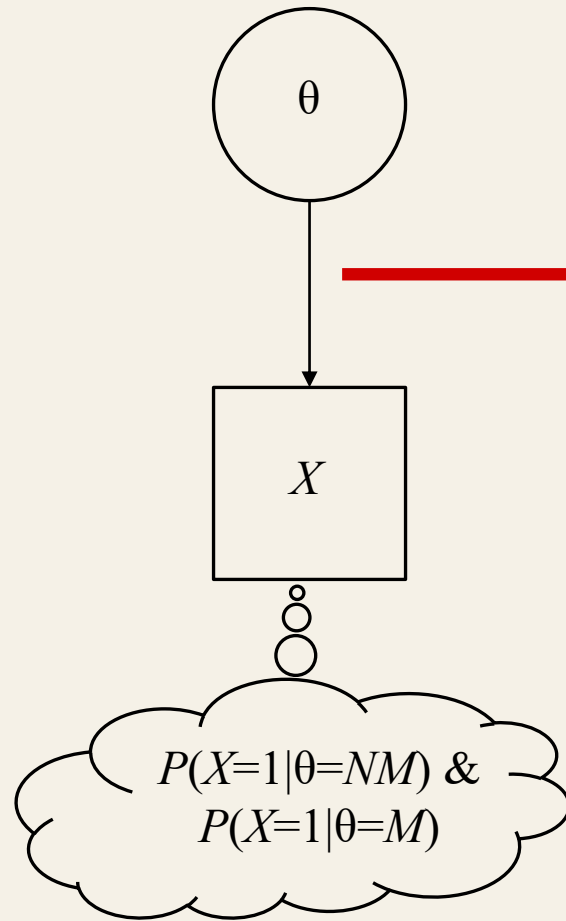
- Bayesian networks (BN) represent a set of conditional dependencies between a collection of random variables.
- More concretely, models the probability of a state conditioned on a set of observed states
- Typically represented as a directed, acyclical graphical model (DAG)
 - Nice, tidy way to represent the joint distribution over the set of variables
- Bayes theorem (Bayes, 1763) provides the mechanism for updating our beliefs as evidence is accumulated

Bayesian Networks

- BNs represent a very general, flexible framework
 - LCA, DCM, state-space models (e.g., hidden Markov models, particle filters), etc. are all a special case of a BN
- Advantages of BNs (Almond et al., 2015):
 - Computationally efficient (exploit conditional independence assumptions)
 - Modular
 - Can handle very complex models/systems of variables
 - Can provide real-time feedback/updating
 - Can be used in mixed-methods designs (e.g., incorporate expert knowledge)
 - And many more!

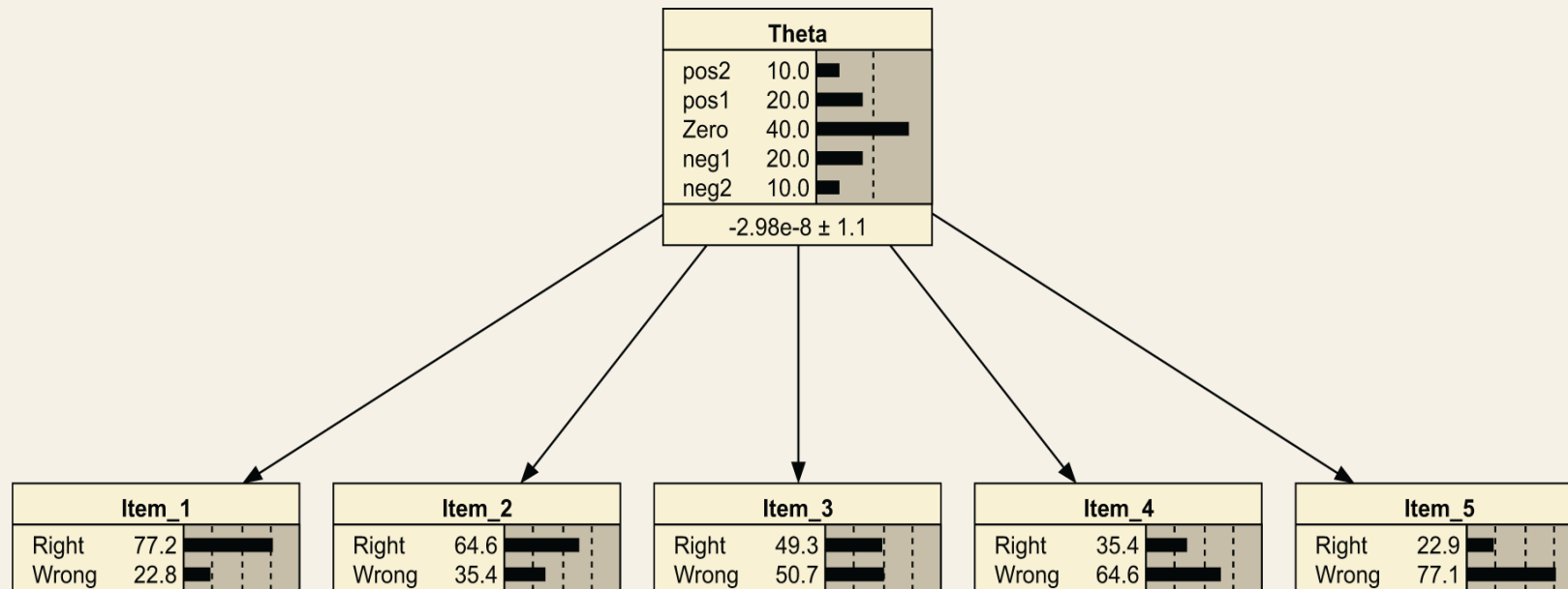
$\theta: \{master, non-master\}$
 $X: \{correct, incorrect\}$

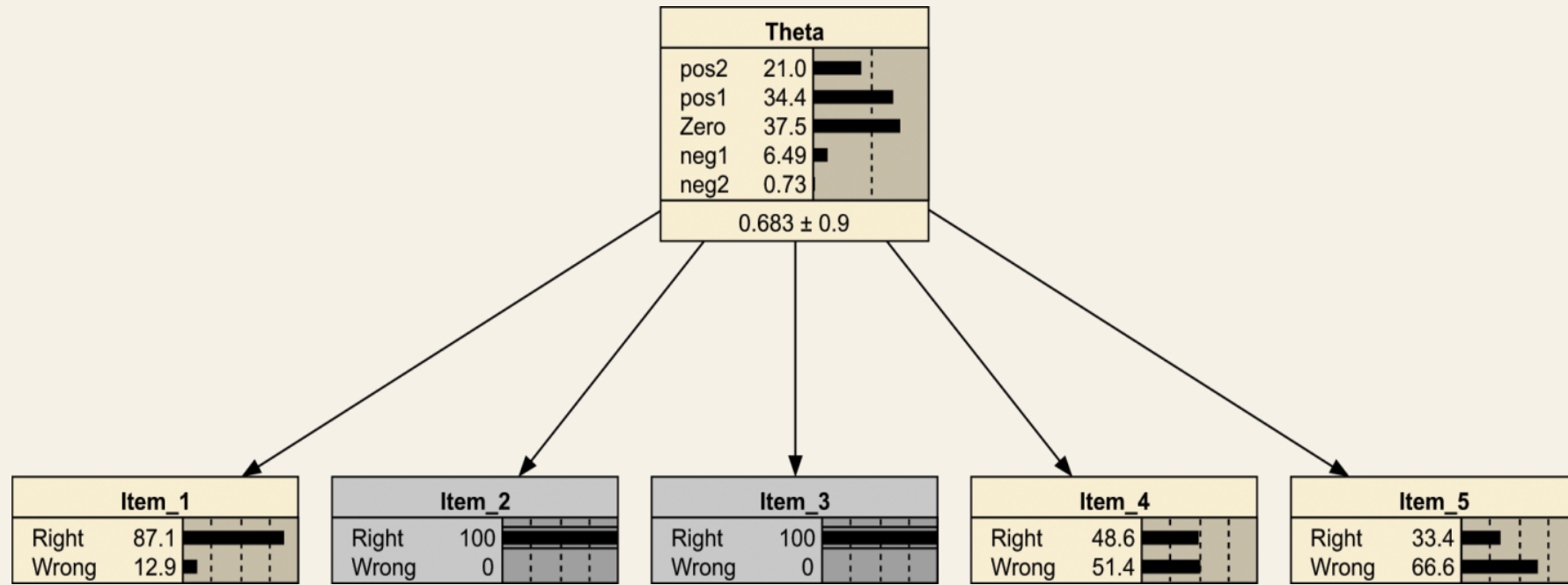


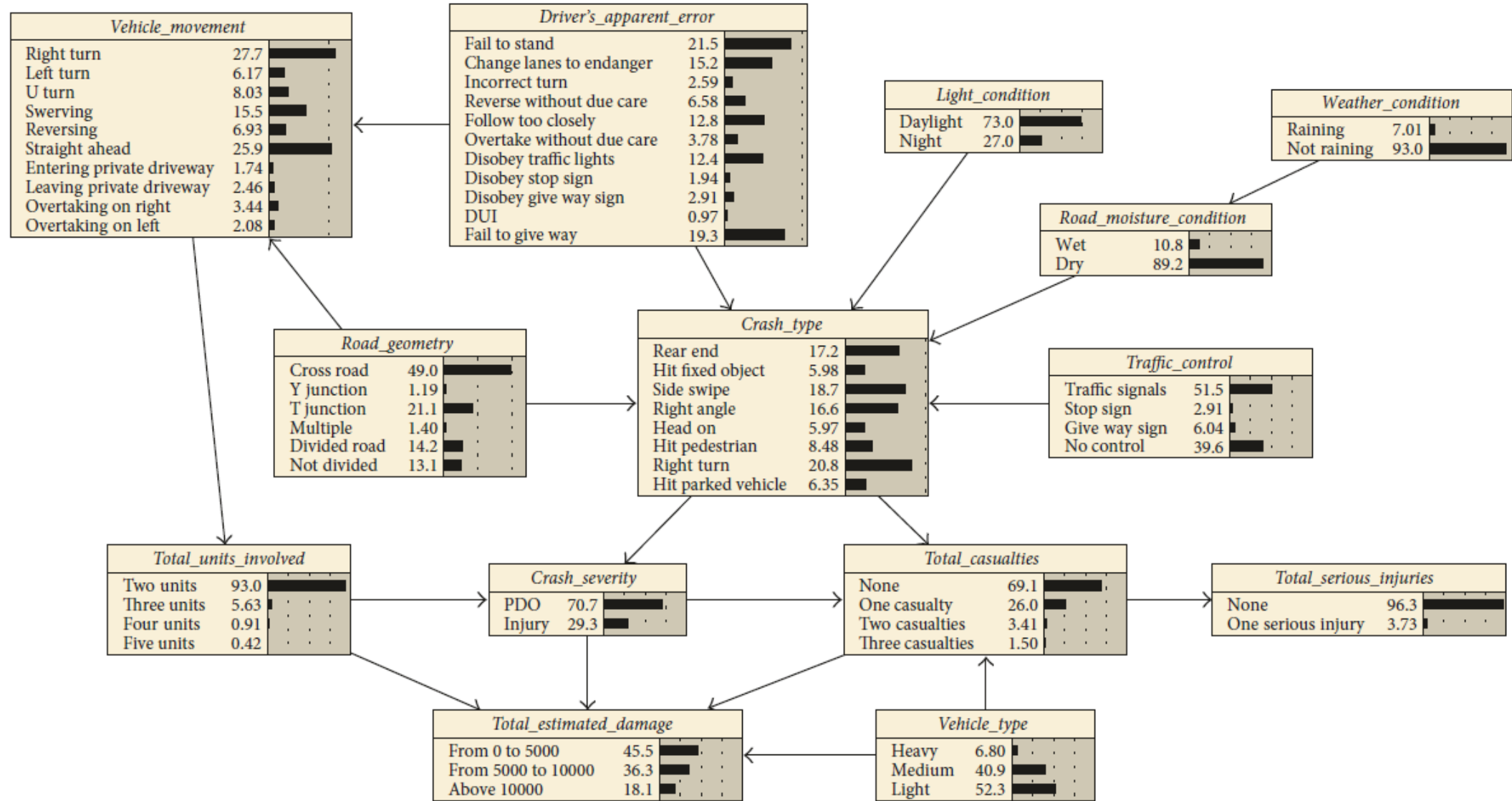


Highly discriminating item; Low uncertainty		
	$\theta = NM$	$\theta = M$
$X=0$	0.95	0.05
$X=1$	0.05	0.95
Non-discriminating; maximal uncertainty		
	$\theta = NM$	$\theta = M$
$X=0$	0.50	0.50
$X=1$	0.50	0.50

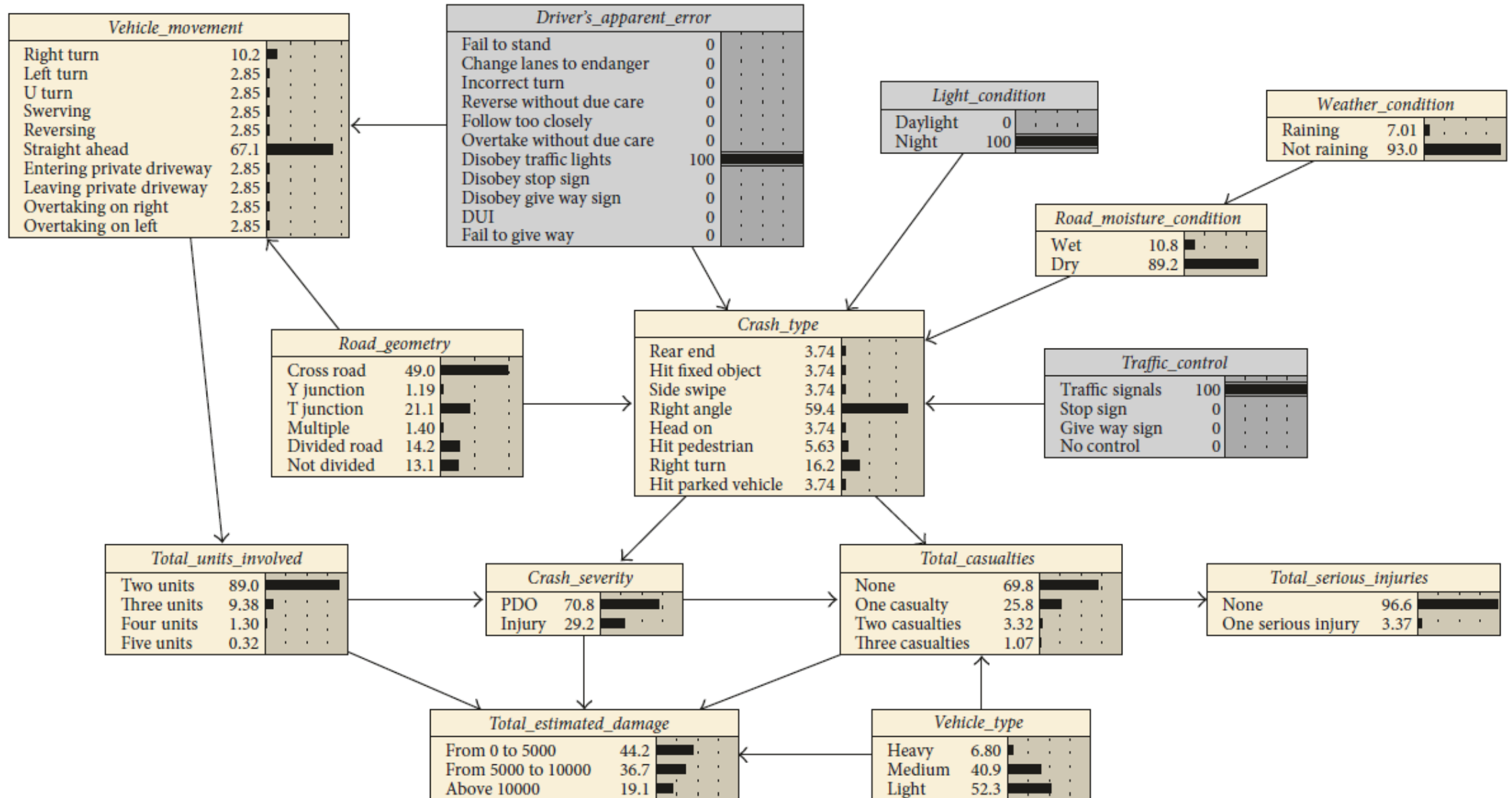
Bayesian Networks - Examples

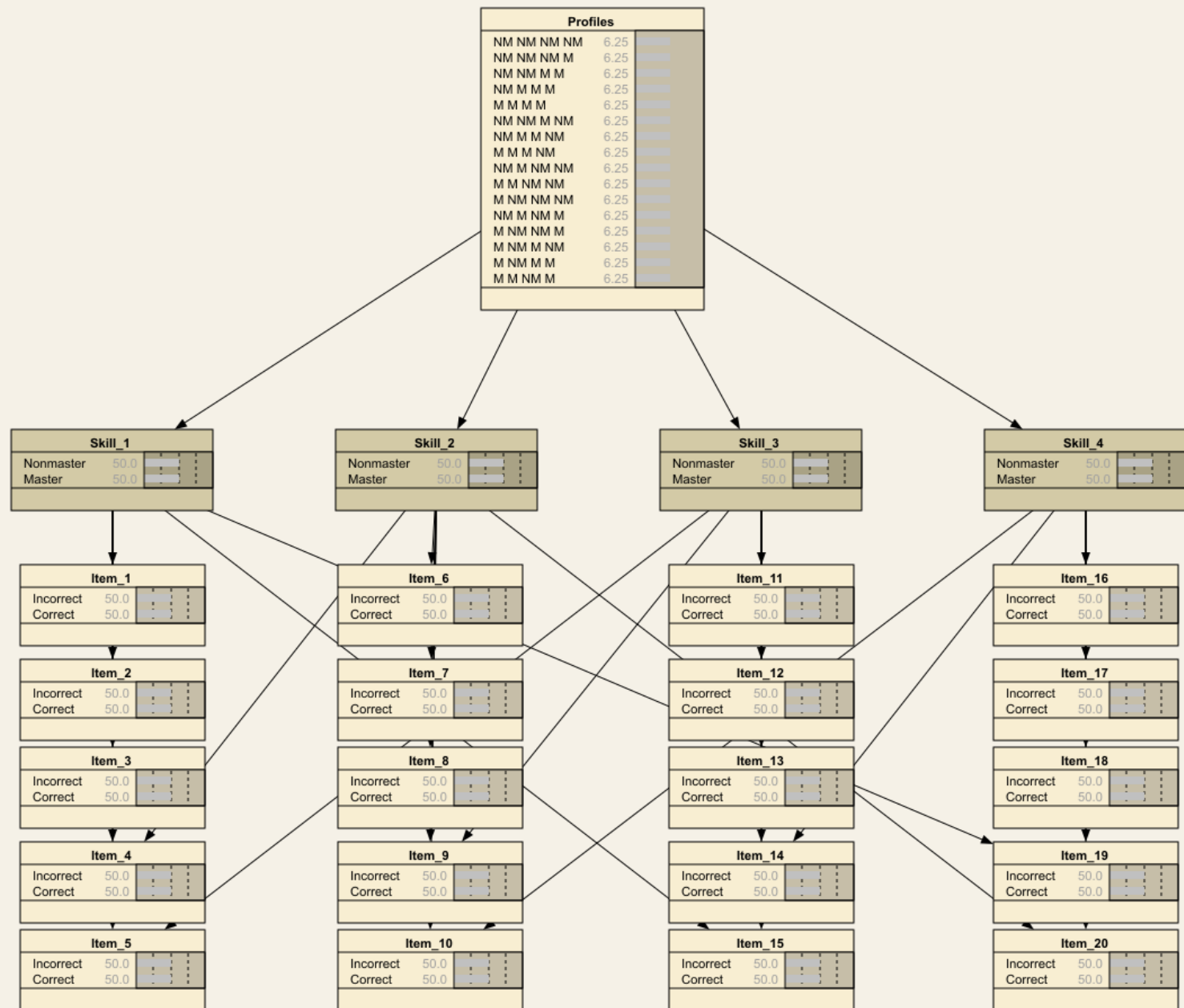






Source: Zou & Yue (2017)





DCM vs BN

- DCMs are much more common in practice due to a much longer history in the educational/psychological literature
- BNs are the more flexible and computationally efficient of the two
 - Preferred for very large systems of variables
- There is a rich literature on BN in computer science (e.g., intelligent tutoring systems) and fields such as genomics, but these models are a relatively recent advancement in educational/psychological assessment

DCM vs BN

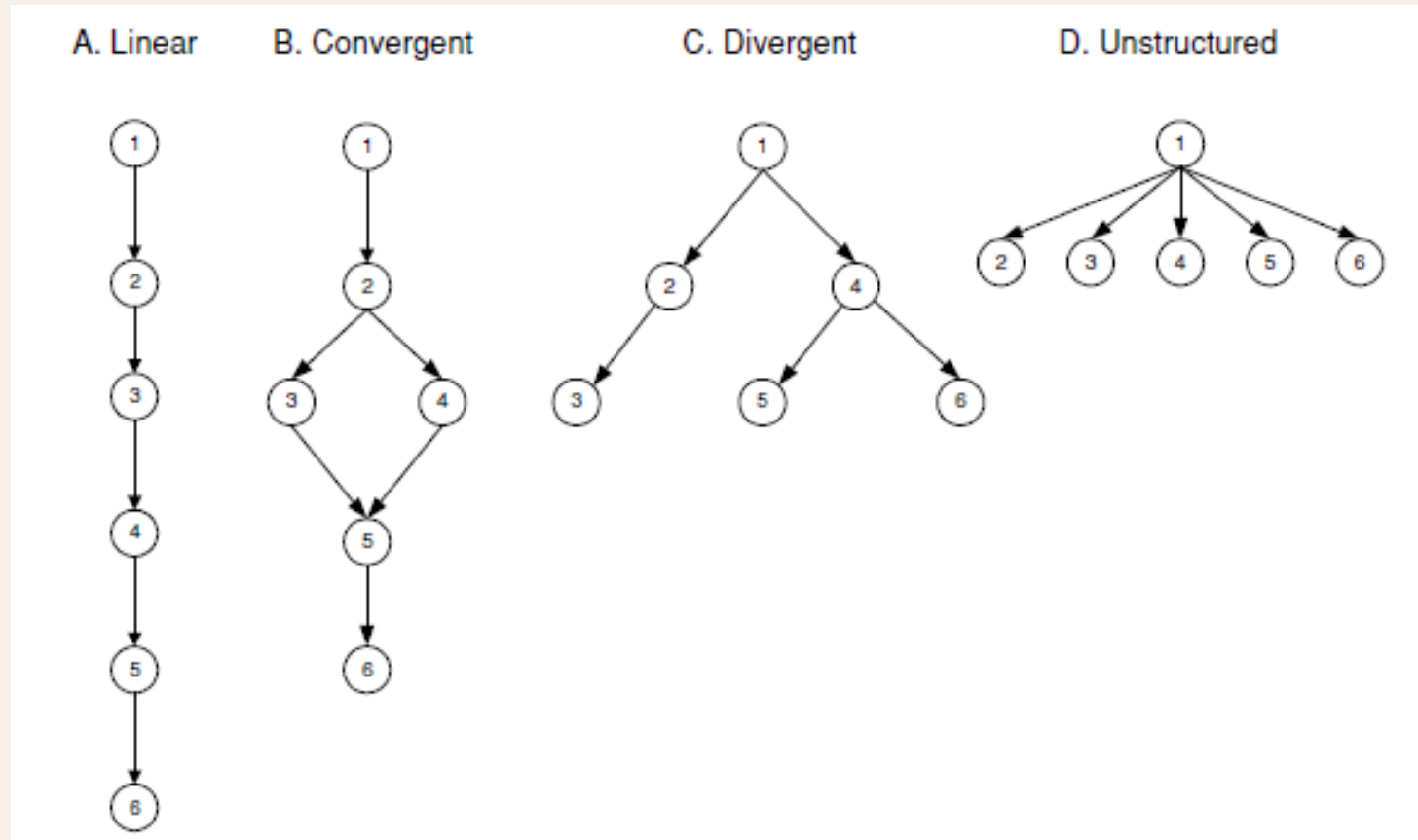
- There may be more opportunity to receive training on DCMs
 - I'm not aware of any graduate courses on BNs being offered in the social sciences
 - Though NCME offers pre-conference workshops on both topics most years
- BNs lend themselves well to graphical representations, which can help to make the resulting inferences more interpretable (Almond et al., 2007)
- For longitudinal applications, the BN framework (i.e., dynamic Bayesian networks; DBN) tends to be preferred*

How can these models be extended?

Modeling Learning Progressions

- “...descriptions of successively more sophisticated ways of thinking about a topic that can follow one another... over time” (National Research Council, 2007)
- There are several ways to operationalize this concept
- Learning progressions are typically represented as attribute hierarchies
- Attribute hierarchies are defined by the relationships between the attributes and specify which attribute profiles should/should not be observed in the population (Rupp, Templin, & Henson, 2010)

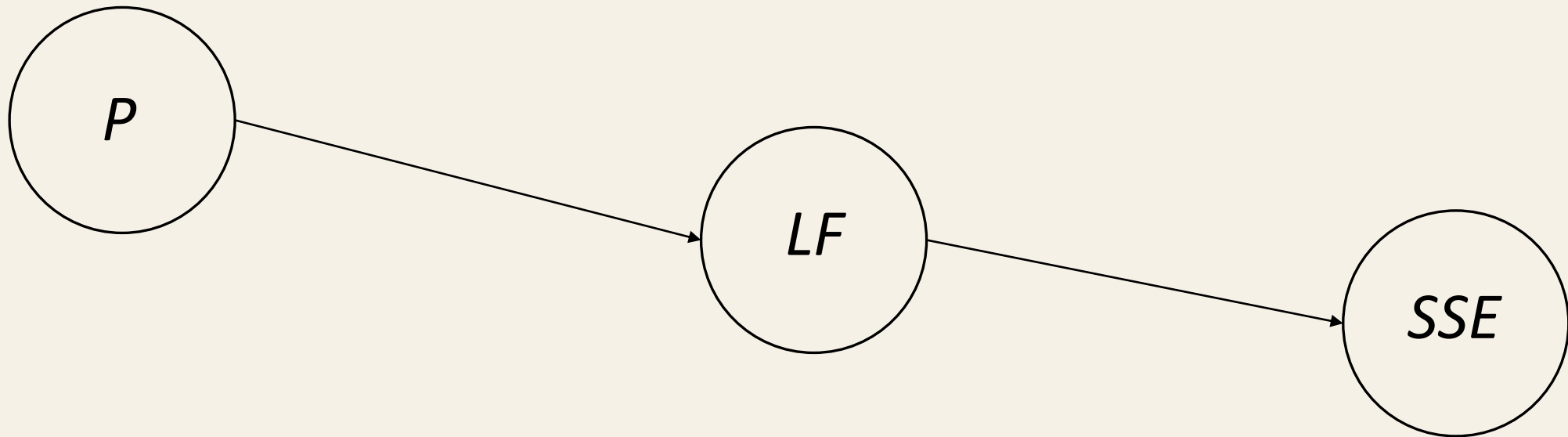
Modeling Learning Progressions



Source: Gierls, Leighton, & Hunka (2007)

Modeling Learning Progressions

- Suppose we have three skills we want to model related to solving linear functions: Prerequisites (P), understanding linear functions (LF), and solving systems of equations (SSE)



Modeling Learning Progressions

- We have $2^3 = 8$ possible profiles:

[0,0,0]	[1,0,0]
[0,0,1]	[1,1,0]
[0,1,0]	[1,0,1]
[0,1,1]	[1,1,1]

Modeling Learning Progressions

- But...

[0,0,0]	[1,0,0]
[0,0,1]	[1,1,0]
[0,1,0]	[1,0,1]
[0,1,1]	[1,1,1]

- We would fix the probability of these profiles to zero

Modeling Growth

- We're often interested in skill progression, not just skill status.
- Both the DCM and BN frameworks offer longitudinal extensions.
- These extensions model the change in both skill category (e.g., mastery) and attribute profiles.
- Very little research (empirical or methodological) has been done examining these models in psychometric contexts.
 - If you're a graduate student, this sentence might be important to you.
 - If you think BNs seem exciting and are interested in growth modeling, my office is LPH 269. I have tea available.

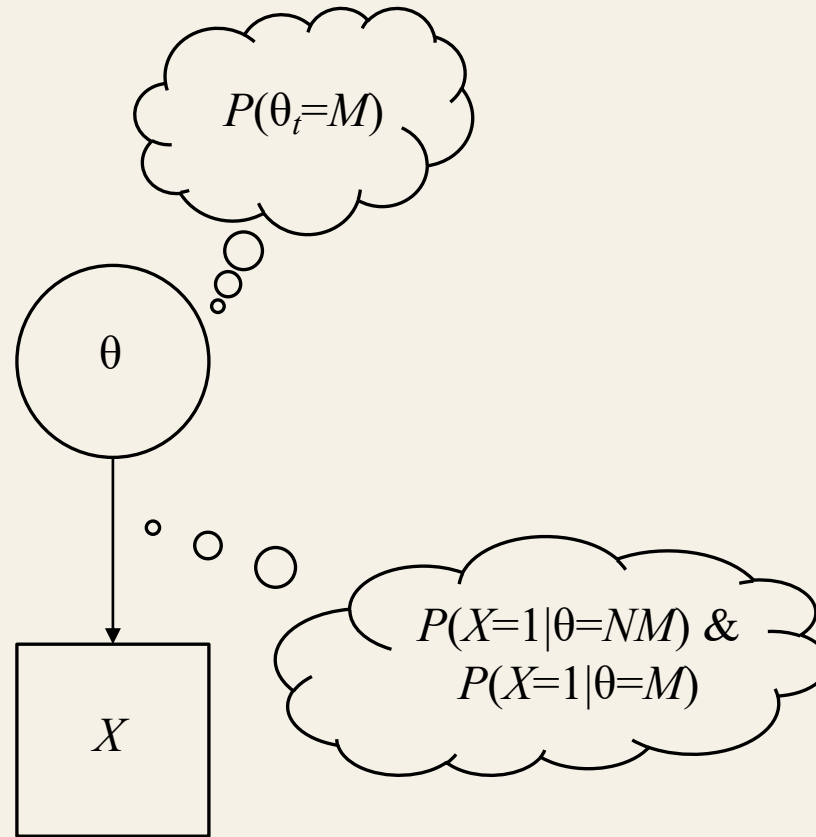
Modeling Growth – L-DCMs

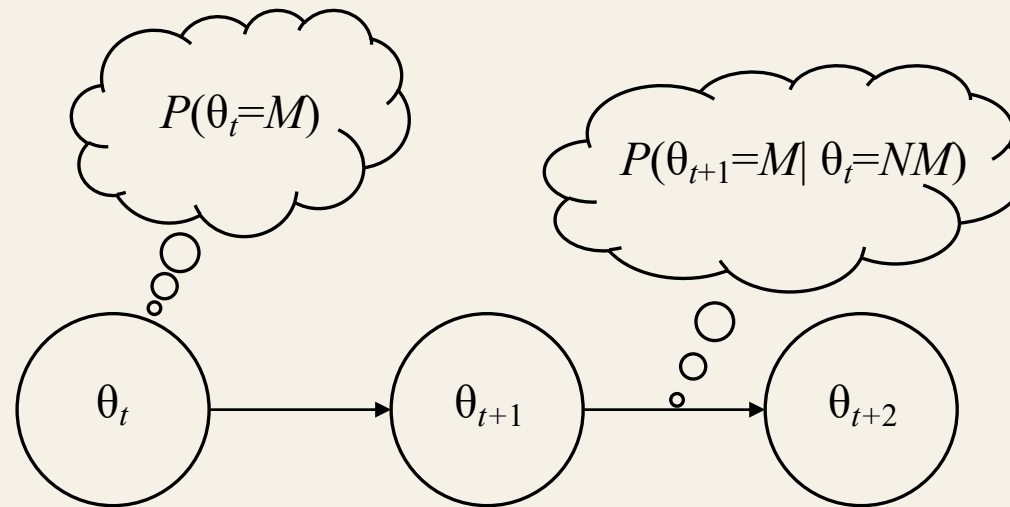
- Latent-transition model-based methods (e.g., Kaya & Liete, 2017; Madison & Bradshaw, 2018)
 - Akin to confirmatory, restricted LTA models
 - Currently only used for pre/post designs (i.e., $T=2$)
- Higher-order DCMs (e.g., de la Torre & Douglas, 2004; Templin & Bradshaw, 2014)
 - Uses a continuous, higher-order factor
- Multivariate Longitudinal DCM (Pan, Qin, & Kingston, 2020)
 - Loglinear DCM (LDCM) measurement model with a multivariate growth curve component

Modeling Growth – DBNs

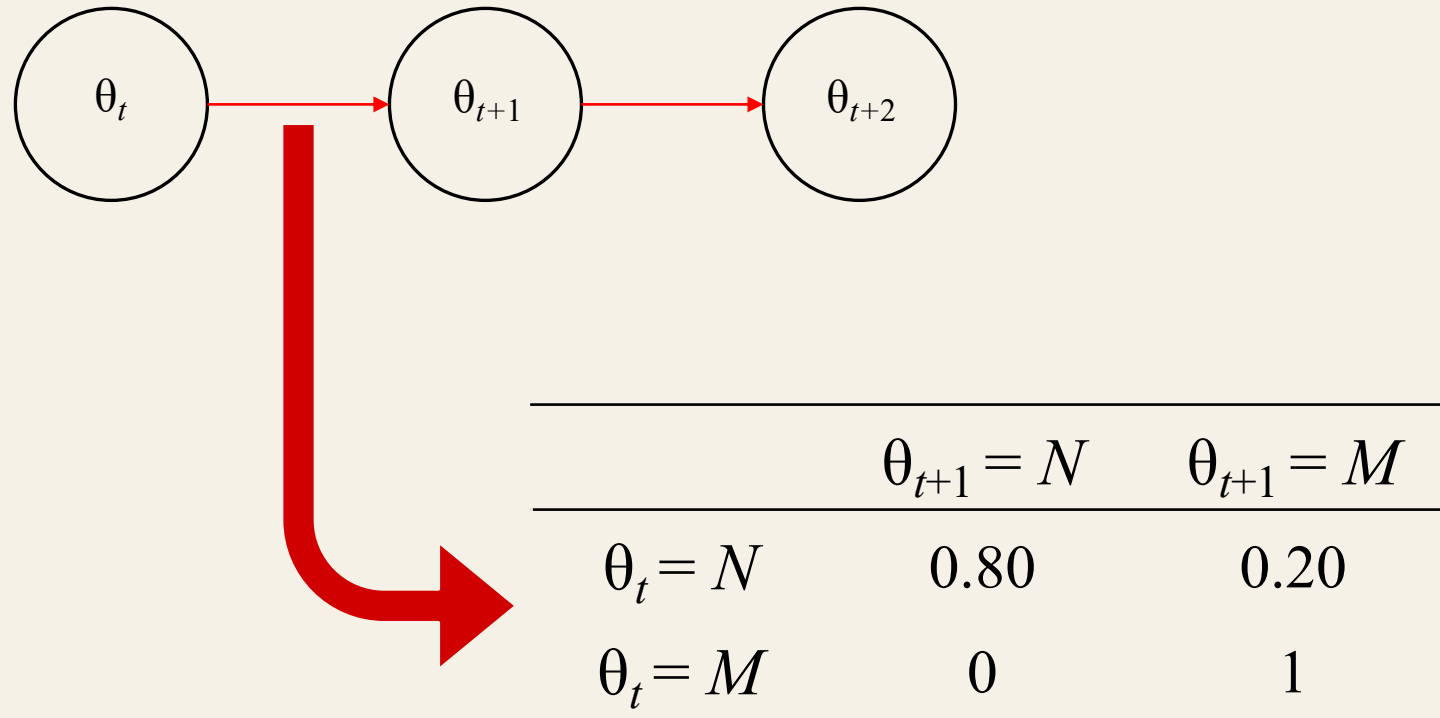
- Longitudinal extension of a Bayesian network (BN).
- A series of time-specific BNs connected by a “spine” which bridges the gap between the time slices.
- Can be used to model an individual’s propensity to transition from one profile to another over time.
- Maintain the same advantages as BNs (efficiency, flexibility, etc.; see Reichenberg, 2018)

$\theta: \{master, non-master\}$
 $X: \{correct, incorrect\}$

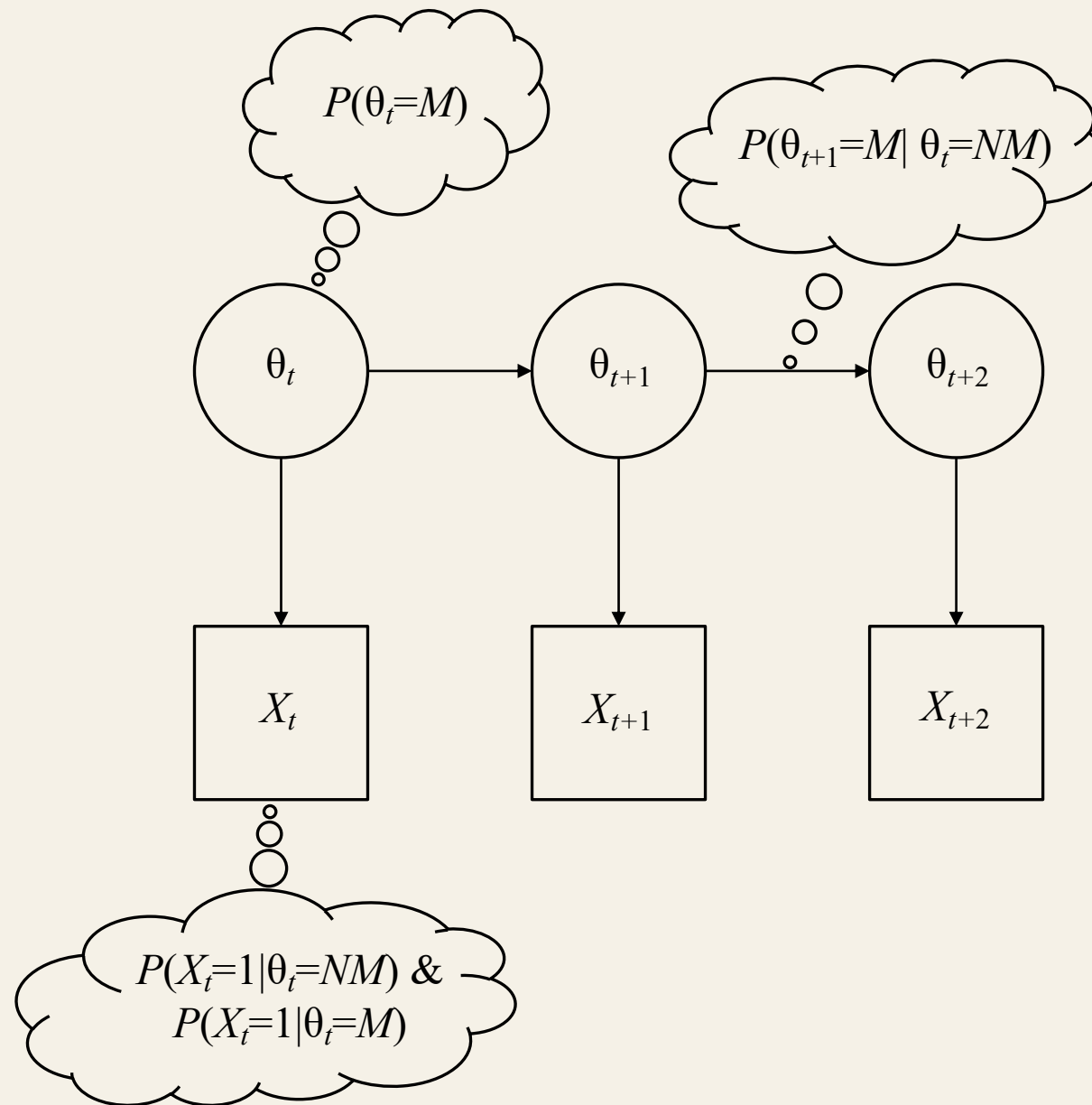


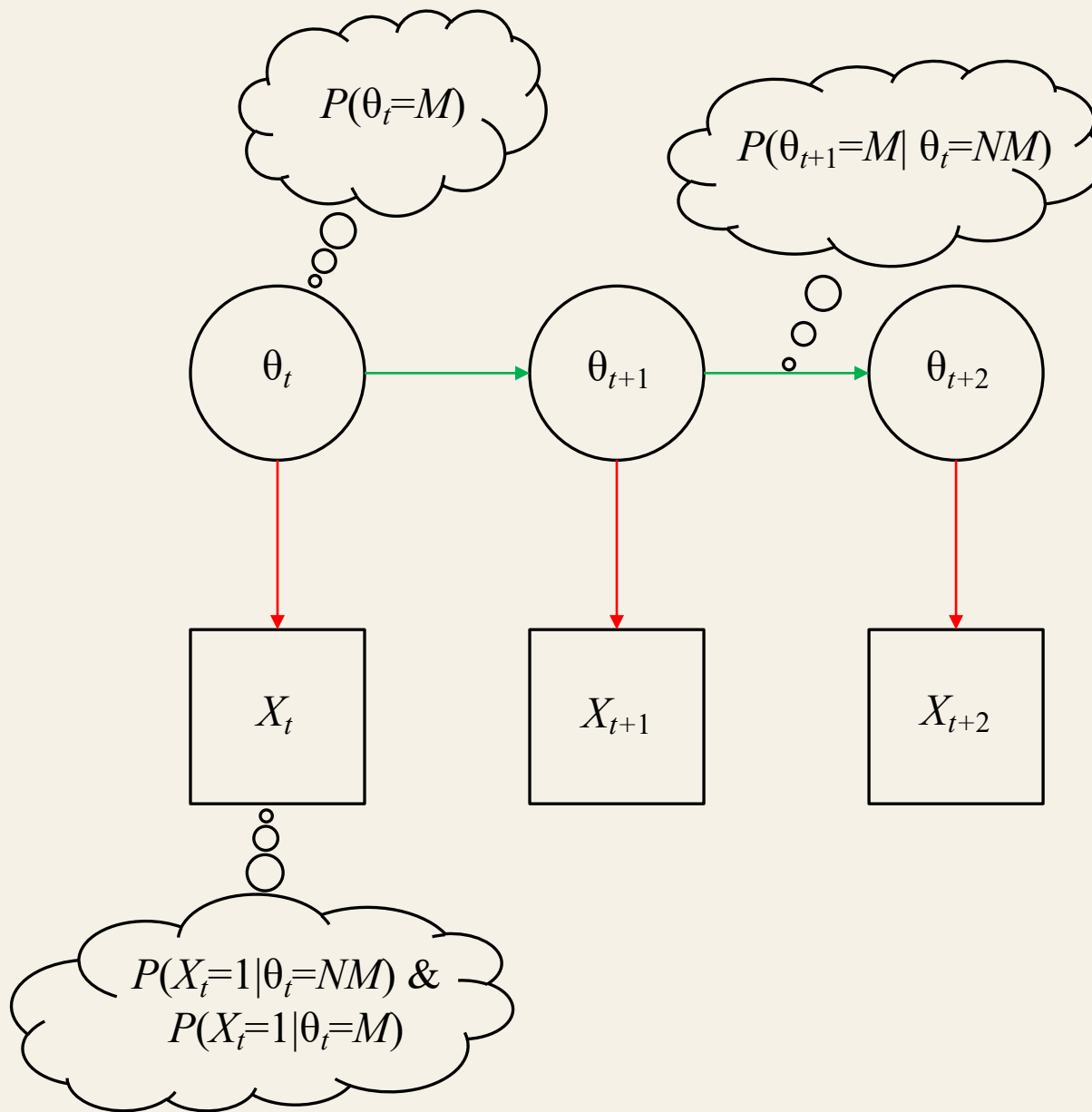


- The longitudinal aspect of the model is defined by the *transition matrix*, not unlike in a latent transition model.

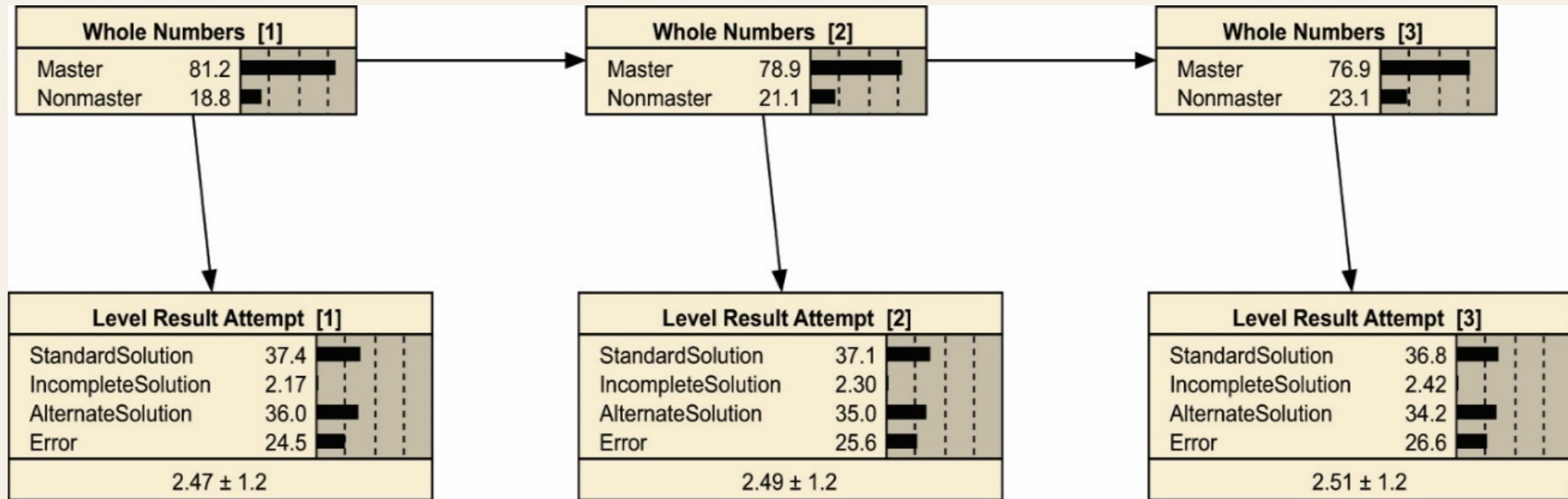


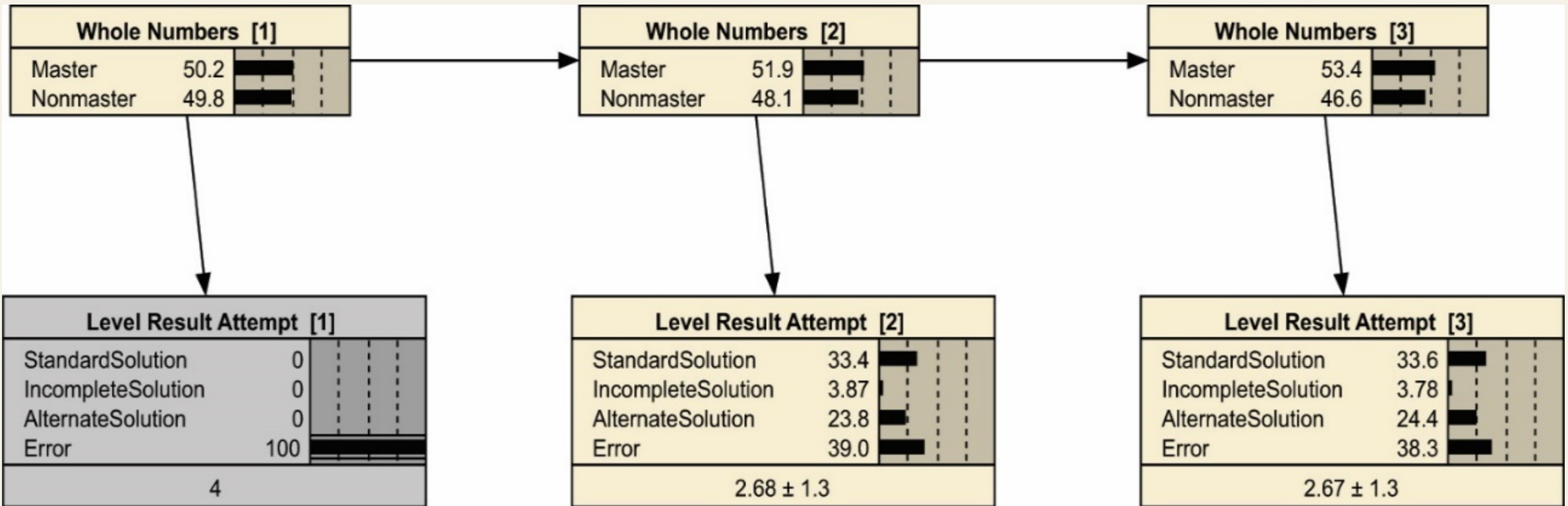
Note. N denotes non-mastery while M denotes mastery.

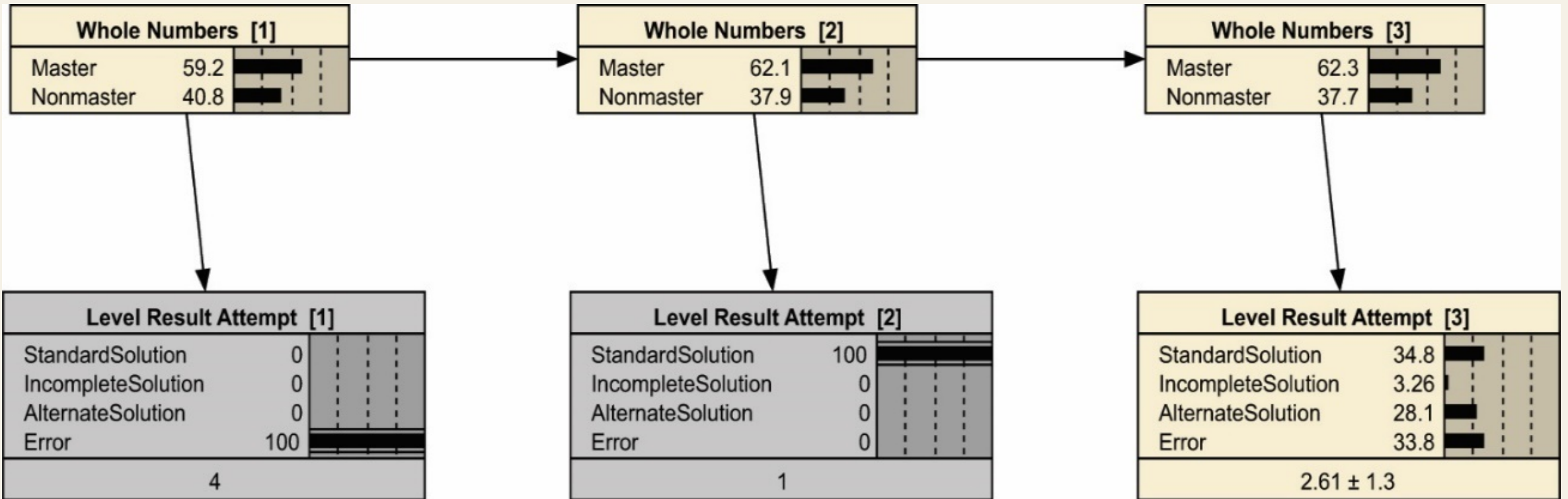


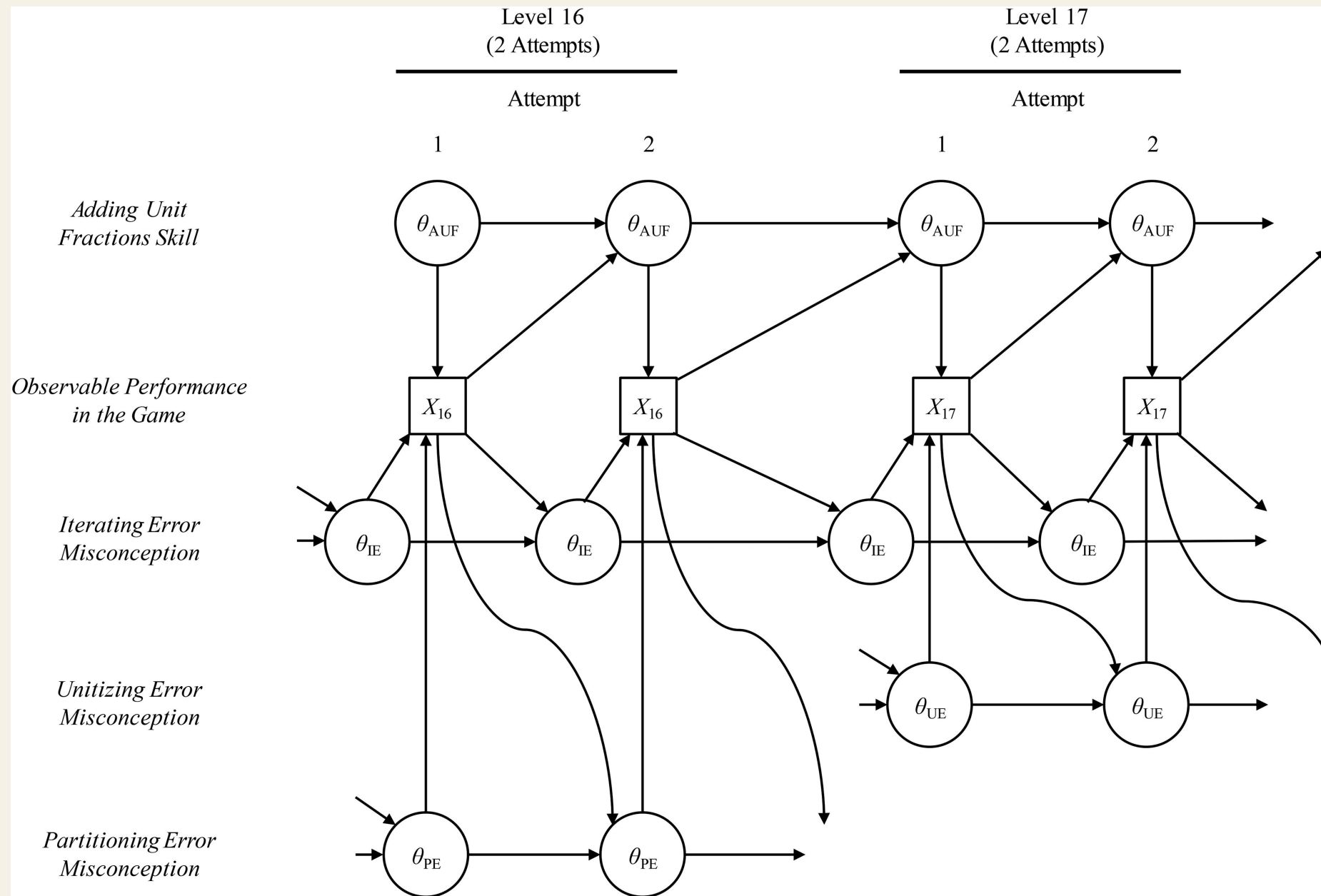


Example DBN

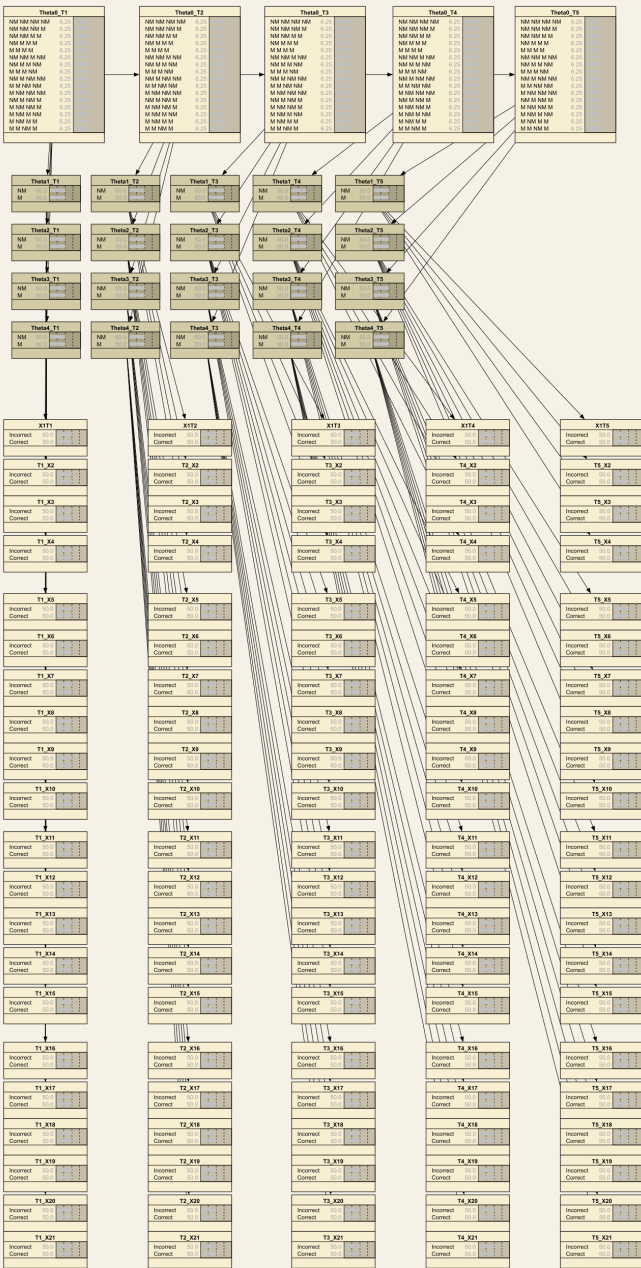


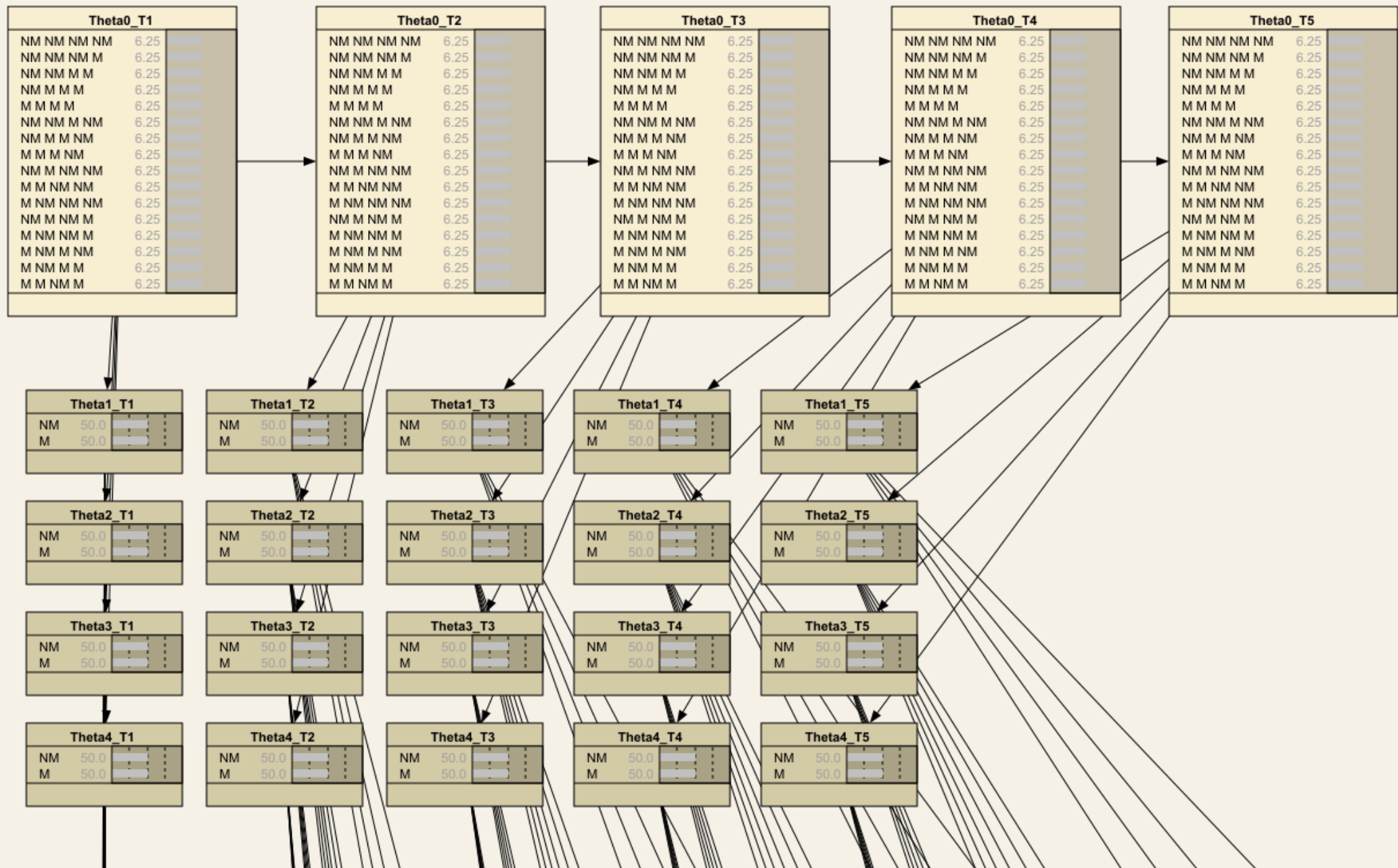


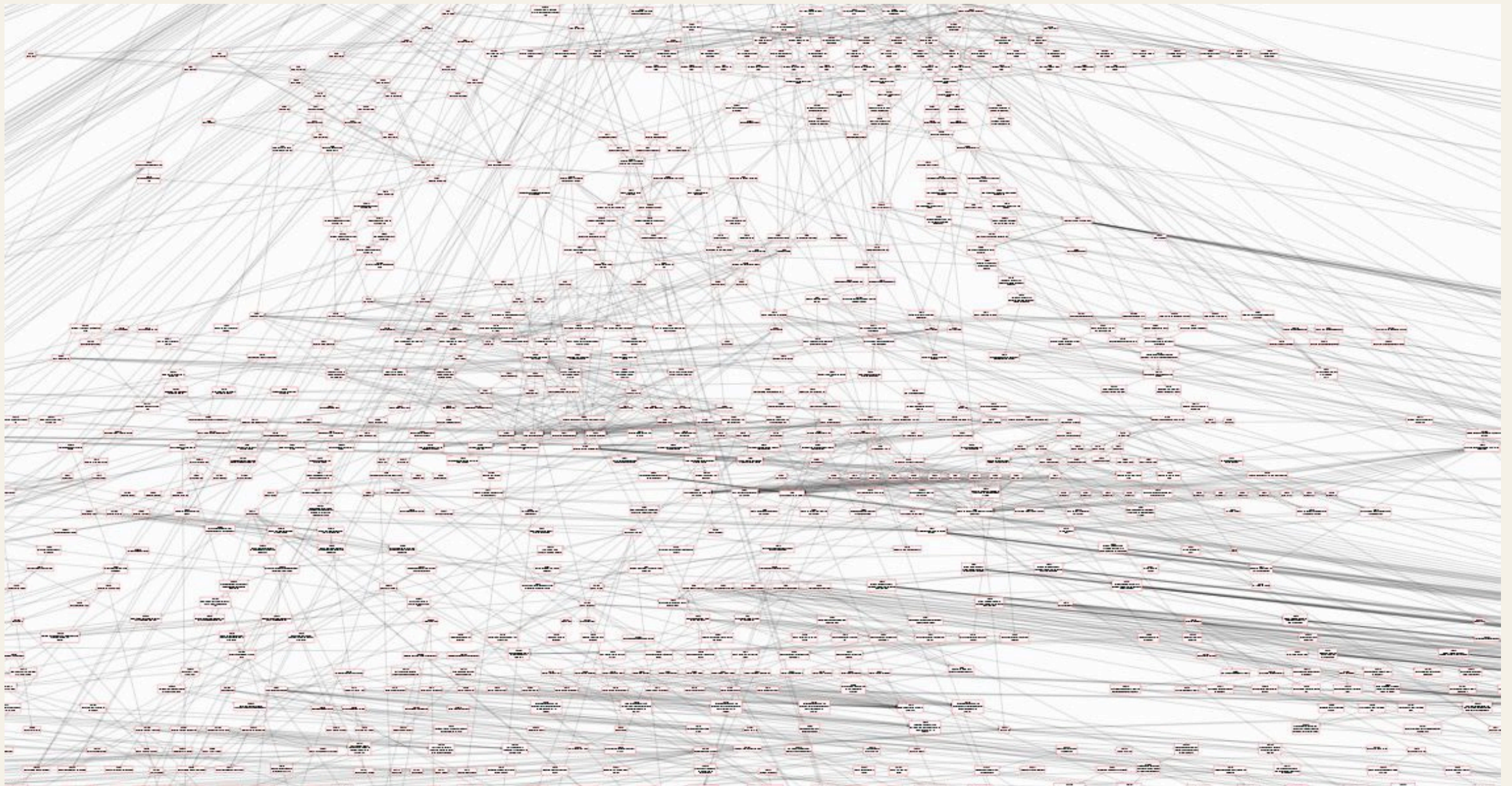




Source: Levy (2019)







Source: www.dynamiclearningmaps.org

Software

Software Options - DCMs

- [Mplus](#) (see Templin & Hoffman, 2013)
- [flexMIRT](#)
- R
 - *CDM* package
 - *GDINA* package
- von Davier & Lee (2019) offers chapters specific to each of these options

Software Options - BNs

- [Netica](#) (\$)
- [BayesiaLab](#) (\$)
- [Hugin](#) (\$)
- [GeNIe](#)
- [BayesServer](#) (\$)
- [MSNBx](#) (no longer supported)

Software Options - BNs

- R
 - [bnlearn](#)
 - GeNIe has an R interface (rSMILE) for use with their SMILE API
 - Netica can interface with R using the [rNETICA](#) package (limited support)
 - Other API (e.g., BayesiaLab) can be used by calling Java/C from with R
- Python
 - [BayesPy](#)
- Probabilistic Programming Languages
 - [JAGS](#)
 - [WinBUGS/OpenBUGS](#)
 - [Stan](#)

Where can I find more information?






Resources

- Textbooks:

- Rupp, A.A., Templin, J. & Henson, R.A. (2010). *Diagnostic Measurement: Theory, Methods, and Applications*. Guilford.
- von Davier, M. & Lee, Y.S. (Eds.). (2019). *Handbook of Diagnostic Classification Models: Models and Model Extensions, Applications, Software Packages*. Springer.
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- Nielsen, T.D. & Jensen, F.V. (2009). *Bayesian Networks and Decision Graphs*. Springer.

- [Diagnostic measurement public database](#)

- [BN examples](#)

- Mplus  / R  code for simple DCM and Netica  / GeNIe  file for equivalent BN
 - Sample data for model fitting  (.csv)



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